The Malthusian Hypothesis

Oded Galor

October 26, 2019

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- The Malthusian epoch is key to the resolution of the two mysteries

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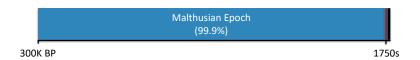
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- The Post-Malthusian Regime

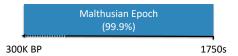
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Phases of Development: Timeline of the Most Developed Economies

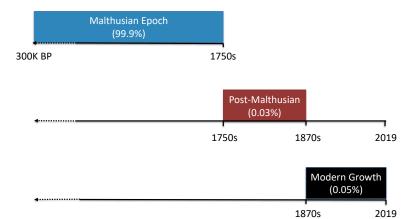


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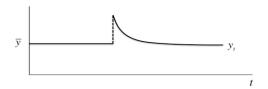
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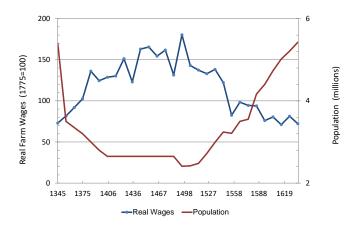
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 - No impact on income per capita (real wages)

Malthusian Adjustments to the Black Death: England, 1348–1635



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 - 180 years (Chaney and Hornbeck, EJ 2016)

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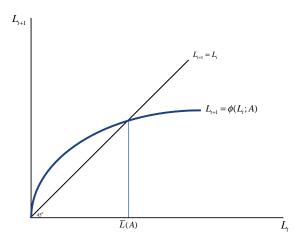
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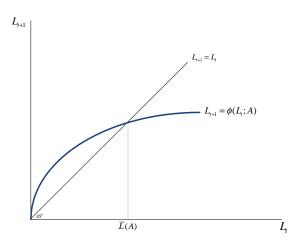
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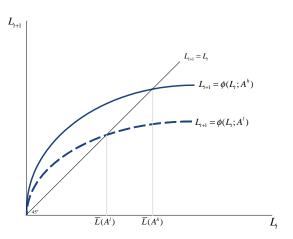
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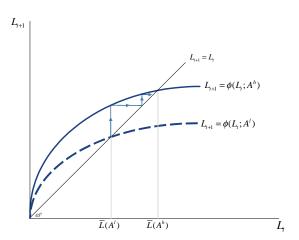
Population Dynamics



Adjustment of Population to Advancements in Technology



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• The time path of income per worker

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where

$$n_t = \frac{\gamma}{\rho} y_t$$

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 \Longrightarrow

$$y_{t+1} = rac{y_t}{n_t^{lpha}} = rac{y_t}{\left[rac{\gamma}{
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 \Rightarrow

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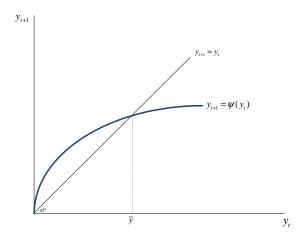
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$$y_{t+1} = \left[rac{
ho}{\gamma}
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• The time path of income per worker

$$y_{t+1} = \left[rac{
ho}{\gamma}
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• Steady-State $y_{t+1} = y_t = \bar{y}$

$$\bar{y} =$$

The time path of income per worker

$$y_{t+1} = \left[\frac{\rho}{\gamma}\right]^{\alpha} y_t^{1-\alpha}$$

• Steady-State $y_{t+1} = y_t = \bar{y}$

$$ar{y} = \left[rac{
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The steady-state level of income per worker

$$\bar{y} =$$

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The steady-state level of income per worker

$$\bar{y} = \left[\frac{\rho}{\gamma}\right]$$

The steady-state level of fertility

$$\bar{n} = \frac{\gamma}{\rho}\bar{y} =$$

• The time path of income per worker

$$y_{t+1} = \left[\frac{\rho}{\gamma}\right]^{\alpha} y_t^{1-\alpha}$$

• Steady-State $y_{t+1} = y_t = \bar{y}$

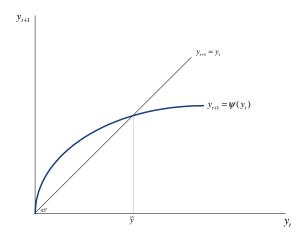
$$\bar{y} = \left[\frac{\rho}{\gamma}\right]^{\alpha} \bar{y}^{1-\alpha}$$

The steady-state level of income per worker

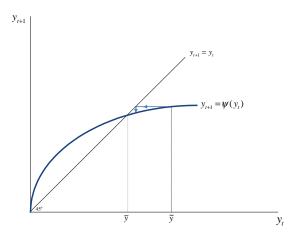
$$\bar{y} = \left[\frac{\rho}{\gamma}\right]$$

• The steady-state level of fertility

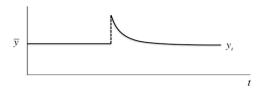
$$ar{n} = rac{\gamma}{
ho}ar{y} = \left[rac{\gamma}{
ho}
ight]\left[rac{
ho}{\gamma}
ight] = 1$$



The Effect of Technological Advancement on income per Worker



Technological Progress and the Time Path of Population & Income





Impact of Technological Progress or Land Productivity

Increases the working population in the short-run and long-run

$$\frac{\partial L_t}{\partial A} > 0$$
; $\frac{\partial L_t}{\partial X} > 0$; $\frac{\partial \bar{L}}{\partial A} > 0$; $\frac{\partial \bar{L}}{\partial X} > 0$;

Increases income per worker in the short-run but not in the long-run

$$\frac{\partial y_t}{\partial A} > 0$$
; $\frac{\partial y_t}{\partial X} > 0$; $\frac{\partial \bar{y}}{\partial A} = 0$; $\frac{\partial \bar{y}}{\partial X} = 0$

• Technological progress:

- Technological progress:
 - Higher population density

- Technological progress:
 - Higher population density
 - No effect on income per-capita in the long-run

- Technological progress:
 - Higher population density
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- Higher land quality:

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Objective

• Confirm (or refute) the Malthusian hypothesis:

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 - The causal effect of technology on Population

- Confirm (or refute) the Malthusian hypothesis:
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 - The absence of an effect of technology on income per capita

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 - The causal effect of technology on Population
 - The absence of an effect of technology on income per capita
- Confirmation cannot rely on *correlation* between technology & population:
 - Correlation
 ⇒ Malthusian impact of technology on population

- Confirm (or refute) the Malthusian hypothesis:
 - The causal effect of technology on Population
 - The absence of an effect of technology on income per capita
- Confirmation cannot rely on *correlation* between technology & population:
 - - May reflect the impact of population on technology

Correlation ⇒ Causation

- Correlation ⇒ Causation
 - Reverse Causality

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 - Reverse Causality
 - Omitted Variables

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- Correlation ⇒ Causation
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 - Correlation between: [overweight people] & [people on diet]

- Correlation ⇒ Causation
 - Reverse Causality
 - Omitted Variables
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 - Correlation between: [overweight people] & [people on diet]
 - Diet ⇒ Overweight ?

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- Omitted Variables (3rd factor governs the correlation):

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 - Correlation between: [overweight people] & [people on diet]
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 - Overweight \Longrightarrow Diet
- Omitted Variables (3rd factor governs the correlation):
 - Correlation between: [ice cream consumption] & [people drown]

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 - [ice cream consumption] ⇒ [people drown] ?

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 - [ice cream consumption] ⇒ [people drown]?
 - high temperature

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 - high temperature ⇒ [swimming in sea ↑]

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 - [ice cream consumption] ⇒ [people drown]?
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 - high temperature \Rightarrow [swimming in sea \uparrow] \Rightarrow [people drown \uparrow]

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Identification Strategy

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Identification Strategy

- Exploit exogenous sources of cross-country variation in technological level
 - Historical origins of variation in technological level across countries
 - Differential onset of the Neolithic Revolution across the globe

• The transition from hunter-gatherer tribes to agricultural communities

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 - Emergence of non-food-producing class:

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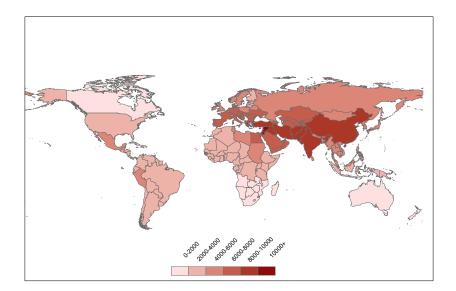
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The Neolithic Revolution

- The transition from hunter-gatherer tribes to agricultural communities
 - Emergence of non-food-producing class:
 - Knowledge creation (science, technology & written languages)
 - ⇒ Technological head start
- Variations in the timing of the NR:
 - \Longrightarrow Origins of variations in the level of technology across the globe

Variation in the Onset of the Neolithic Revolution



Geographical factors conducive for biodiversity (climate, latitude, landmass)

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 Something
 Onset of domestication

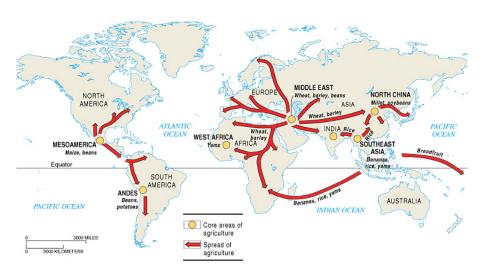
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 - Availability of domesticable species of plants and animals
 - Sometimes of domestication
- Orientation of continents:
 - \Longrightarrow Diffusion of agricultural practices along similar latitudes
- Climatic changes
 - Hunter-gatherers abandoned their traditional nomadism in order to store food and smooth their consumption (Matranga, 2019)

Spatial Diffusion of the Neolithic Revolution



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- The domination of Euro-Asia in the pre-colonial era reflects:
 - Larger number of domesticable species of plants and animals
 - East-West orientation
 - Technological head start and its effect on development
- Earlier onset of the Neolithic Revolution:
 - Technological superiority

Avoiding reverse causality:

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 - Exploit the projected level of technology in each country (rather than the actual one) based on:

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 - Instrumental Variable (IV) for the timing of the NR
 - Number of prehistoric domesticable species of plants and animals
 - Identifying Assumption: prehistoric domesticable species of plants and animals affected population density only via the NR timing

The Neolithic Revolution & Technological Level: 1000 BCE-1500 CE

	(1)	(2)	(3)	(4)	(5)	(6)	
	OLS	OLS	OLS	OLS	OLS	OLS	
	Log Technological Level						
	1000 BCE 1 CE 1500 CE						
Log years since Neolithic	0.72*** (0.06)	0.47*** (0.12)	0.56*** (0.06)	0.28** (0.12)	0.74*** (0.06)	0.34** (0.10)	
Geographical Controls	No	Yes	No	Yes	No	Yes	
Continental dummies	No	Yes	No	Yes	No	Yes	
Observations	112	112	134	134	134	134	
Adjusted R ²	0.51	0.60	0.31	0.63	0.55	0.82	
Notes: Robus	t standard erro	ors in parenthe	ses; *** p<0.	01, ** p<0.0	5, * p<0.1		

$$\ln P_{i,t} = \alpha_{0,t} + \alpha_{1,t} \ln T_{i,t} + \alpha_{2,t} \ln X_i + \alpha'_{3,t} \Gamma_i + \alpha'_{4,t} D_i + \delta_{i,t}$$

$$\ln y_{i,t} = \beta_{0,t} + \beta_{1,t} \ln T_{i,t} + \beta_{2,t} \ln X_i + \beta'_{3,t} \Gamma_i + \beta'_{4,t} D_i + \varepsilon_{i,t}$$

ullet $P_{i,t} \equiv$ population density of country i in year t

$$\ln P_{i,t} = \alpha_{0,t} + \alpha_{1,t} \ln T_{i,t} + \alpha_{2,t} \ln X_i + \alpha_{3,t}^{'} \Gamma_i + \alpha_{4,t}^{'} D_i + \delta_{i,t}$$

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- $X_i \equiv$ measure of land productivity for country i

$$\ln P_{i,t} = \alpha_{0,t} + \alpha_{1,t} \ln T_{i,t} + \alpha_{2,t} \ln X_i + \alpha'_{3,t} \Gamma_i + \alpha'_{4,t} D_i + \delta_{i,t}$$

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- $X_i \equiv$ measure of land productivity for country i
- $\Gamma_i \equiv$ vector of geographical controls for country i

$$\ln P_{i,t} = \alpha_{0,t} + \alpha_{1,t} \ln T_{i,t} + \alpha_{2,t} \ln X_i + \alpha_{3,t}^{'} \Gamma_i + \alpha_{4,t}^{'} D_i + \delta_{i,t}$$

$$\ln y_{i,t} = \beta_{0,t} + \beta_{1,t} \ln T_{i,t} + \beta_{2,t} \ln X_i + \beta_{3,t}^{'} \Gamma_i + \beta_{4,t}^{'} D_i + \varepsilon_{i,t}$$

- $P_{i,t} \equiv$ population density of country i in year t
- $y_{i,t} \equiv$ income per capita of country i in year t
- $T_i \equiv$ years elapsed since the onset of agriculture in country i
- $X_i \equiv$ measure of land productivity for country i
- $\Gamma_i \equiv$ vector of geographical controls for country i
- $D_i \equiv$ vector of continental fixed effect in country i

Determinants of Population Density in 1500 CE

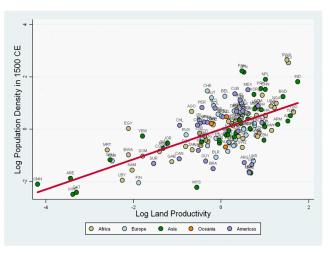
	(1)	(2)	(3)	(4)	(5)	(6)		
	OLS	OLS	OLS	OLS	OLS	IV		
		Log population density in 1500 CE						
Log years since Neolithic	0.833*** (0.298)		1.025*** (0.223)	1.087*** (0.184)	1.389*** (0.224)	2.077*** (0.391)		
Log land productivity		0.587*** (0.071)	0.641*** (0.059)	0.576*** (0.052)	0.573*** (0.095)	0.571*** (0.082)		
Log absolute latitude		-0.425*** (0.124)	-0.353*** (0.104)	-0.314*** (0.103)	-0.278** (0.131)	-0.248** (0.117)		
Distance to nearest coast or river				-0.392*** (0.142)	0.220 (0.346)	0.250 (0.333)		
% land within 100 km of coast or river				0.899*** (0.282)	1.185*** (0.377)	1.350*** (0.380)		
Continental dummies	Yes	Yes	Yes	Yes	Yes	Yes		
Observations	147	147	147	147	96	96		
R^2	0.40	0.60	0.66	0.73	0.73	0.70		
First-stage F-statistic						14.65		
Overident. p-value						0.44		

Effects on Population Density vs Income per Capita

(1)	(2)	(3)	(4)	(5)	(6)
OLS	OLS	OLS	OLS	OLS	OLS
Log Ir	ncome Per Cap	ita in	Log F	opulation Dens	ity in
1500 CE	1000 CE	1 CE	1500 CE	1000 CE	1 CE
0.159 (0.136)	0.073 (0.045)	0.109 (0.072)	1.337** (0.594)	0.832** (0.363)	1.006** (0.483)
0.041 (0.025)	- 0.021 (0.025)	- 0.001 (0.027)	0.584*** (0.159)	0.364*** (0.110)	0.681** (0.255)
-0.041 (0.073)	0.060 (0.147)	-0.175 (0.175)	0.050 (0.463)	-2.140 ** (0.801)	-2.163 ** (0.979)
0.215 (0.198)	-0.111 (0.138)	0.043 (0.159)	-0.429 (1.237)	-0.237 (0.751)	0.118 (0.883)
0.124 (0.145)	-0.150 (0.121)	0.042 (0.127)	1.855 ** (0.820)	1.326 ** (0.615)	0.228 (0.919)
Yes	Yes	Yes	Yes	Yes	Yes
31	26	29	31	26	29
0.66	0.68	0.33	0.88	0.95	0.89
	OLS Log Ir 1500 CE 0.159 (0.136) 0.041 (0.025) -0.041 (0.073) 0.215 (0.198) 0.124 (0.145) Yes 31	OLS OLS Log Income Per Cap 1500 CE 1000 CE 0.159 0.073 (0.045) 0.041 -0.021 (0.025) (0.025) -0.041 0.060 (0.147) 0.215 -0.111 (0.198) (0.138) 0.124 -0.150 (0.145) (0.121) Yes Yes 31 26	OLS OLS Log Income Per Capita in 1500 CE 1000 CE 1 CE 0.159 0.073 0.109 (0.136) (0.045) (0.072) 0.041 -0.021 -0.001 (0.025) (0.025) (0.027) -0.041 0.060 -0.175 (0.073) (0.147) (0.175) 0.215 -0.111 0.043 (0.198) (0.138) (0.159) 0.124 -0.150 0.042 (0.145) (0.121) (0.127) Yes 31 26 29	OLS OLS OLS Log Income Per Capita in Log F 1500 CE 1000 CE 1 CE 1500 CE 0.159 0.073 0.109 1.337** (0.136) (0.045) (0.072) (0.594) 0.041 -0.021 -0.001 0.584*** (0.025) (0.027) (0.159) -0.041 0.060 -0.175 0.050 (0.073) (0.147) (0.175) (0.463) 0.215 -0.111 0.043 -0.429 (0.198) (0.138) (0.159) (1.237) 0.124 -0.150 0.042 1.855** (0.145) (0.121) (0.127) (0.820) Yes Yes Yes Yes 31 26 29 31	OLS OLS OLS OLS Log Income Per Capita in Log Population Dens 1500 CE 1000 CE 1 CE 1500 CE 1000 CE 0.159 0.073 0.109 1.337** 0.832** (0.136) (0.045) (0.072) (0.594) (0.363) 0.041 -0.021 -0.001 0.584*** 0.364*** (0.025) (0.027) (0.159) (0.110) -0.041 0.060 -0.175 0.050 -2.140** (0.073) (0.147) (0.175) (0.463) (0.801) 0.215 -0.111 0.043 -0.429 -0.237 (0.198) (0.138) (0.159) (1.237) (0.751) 0.124 -0.150 0.042 1.855** 1.326** (0.145) (0.121) (0.127) (0.820) (0.615) Yes Yes Yes Yes 31 26 29 31 26

Notes: Robust standard errors in parentheses; *** p<0.01, ** p<0.05, * p<0.1

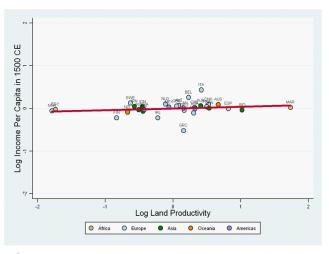
Land Productivity and Population Density in 1500



Conditional on transition timing, geographical factors, and continental fixed effects.

Source: Ashraf-Galor (AER 2011)

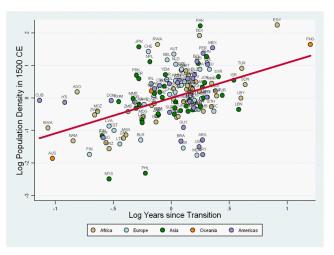
Land Productivity and Income per Capita in 1500



 $Conditional \ on \ transition \ timing, \ geographical \ factors, \ and \ continental \ fixed \ effects.$

Source: Ashraf-Galor (AER 2011)

Technology and Population Density in 1500

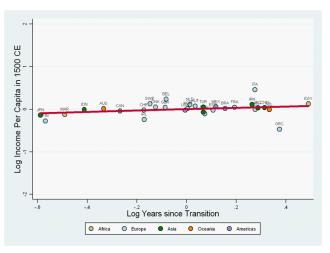


 $Years\ elapsed\ since\ the\ Neolithic\ Transition\ reflects\ the\ technological\ level\ in\ 1500.$

Conditional on land productivity, geographical factors, and continental fixed effects.

Source: Ashraf-Galor (AER 2011)

Technology and Income per Capita in 1500



Years elapsed since the Neolithic Transition reflects the technological level in 1500.

Conditional on land productivity, geographical factors, and continental fixed effects.

Source: Ashraf-Galor (AER 2011)

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• Robustness to the inclusion of direct measures of technology

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Robustness to Direct Measures of Technological Level

	OLS	OLS	OLS	OLS	OLS	OLS
	(1)	(2)	(3)	(4)	(5)	(6)
	_	pulation ity in:	Log Inco			oulation ty in:
	1000 CE	1 CE	Capit 1000 CE	a in: 1 CE	1000 CE	ty in: 1 CE
Log Technology Index in Relevant Period	4.315*** (0.850)	4.216*** (0.745)	0.064 (0.230)	0.678 (0.432)	12.762*** (0.918)	7.461** (3.181)
Log land productivity	0.449*** (0.056)	0.379*** (0.082)	-0.016 (0.030)	0.004 (0.033)	0.429** (0.182)	0.725** (0.303)
Log absolute latitude	-0.283** (0.120)	-0.051 (0.127)	0.036 (0.161)	-0.198 (0.176)	-1.919*** (0.576)	-2.350*** (0.784)
Distance to nearest coast or river	-0.638*** (0.188)	-0.782*** (0.198)	-0.092 (0.144)	0.114 (0.164)	0.609 (0.469)	0.886 (0.904)
% land within 100 km of coast or river	0.385 (0.313)	0.237 (0.329)	-0.156 (0.139)	0.092 (0.136)	1.265**	0.788 (0.934)
Continental dummies Observations	Yes 140	Yes 129	Yes 26	Yes 29 0.30	Yes 26 0.97	Yes 29 0.88

The Causal Effect of Technological Level on Population Density

	OLS	OLS	IV	OLS	OLS	IV
	(1)	(2)	(3)	(4)	(5)	(6)
			Population	Density in:		
		1000CE			1CE	
Log Technology Index in	4.315***	4.198***	14.530***	4.216***	3.947***	10.798***
Relevant Period	(0.850)	(1.164)	(4.437)	(0.745)	(0.983)	(2.857)
Log land productivity	0.449***	0.498***	0.572***	0.379***	0.350**	0.464**
	(0.056)	(0.139)	(0.148)	(0.082)	(0.172)	(0.182)
Log absolute latitude	-0.283**	-0.185	-0.209	-0.051	0.083	-0.052
	(0.120)	(0.151)	(0.209)	(0.127)	(0.170)	(0.214)
Distance to nearest coast or river	-0.638***	-0.363	-1.155*	-0.782***	-0.625	-0.616
	(0.188)	(0.426)	(0.640)	(0.198)	(0.434)	(0.834)
% land within 100 km of coast or river	0.385	0.442	0.153	0.237	0.146	-0.172
	(0.313)	(0.422)	(0.606)	(0.329)	(0.424)	(0.642)
Continental dummies	Yes	Yes	Yes	Yes	Yes	Yes
Observations	140	92	92	129	83	83
R ²	0.61	0.55	0.13	0.62	0.58	0.32
First-stage F-statistic Overid. p-value			12.52 0.941			12.00 0.160

Oded Galor

Robustness to Technology Diffusion and other Geographic Characteristics

	(1)	(2)	(3)	(4)	(5)	(6)
	Log Population Density in 1500		Log Income Per Capita in 1500		Log Population Density in 1500	
Log Technology Index in	0.828*** (0.208)	0.877***	0.117	0.103	1.498**	1.478**
Relevant Period		(0.214)	(0.221)	(0.214)	(0.546)	(0.556)
Log land productivity	0.559***	0.545***	0.036	0.047	0.596***	0.691***
	(0.048)	(0.063)	(0.032)	(0.037)	(0.123)	(0.122)
Log Distance to Frontier	-0.186***	-0.191***	-0.005	-0.001	-0.130*	-0.108*
	(0.035)	(0.036)	(0.011)	(0.013)	(0.066)	(0.055)
Small Island Dummy	0.067	0.086	-0.118	-0.046	1.962**	2.720***
	(0.582)	(0.626)	(0.216)	(0.198)	(0.709)	(0.699)
Landlocked Dummy	0.131	0.119	0.056	0.024	1.490***	1.269***
	(0.209)	(0.203)	(0.084)	(0.101)	(0.293)	(0.282)
% Land in Temperate Climate Zones		-0.196 (0.513)		-0.192 (0.180)		-1.624* (0.917)
Continental dummies	Yes	Yes	Yes	Yes	Yes	Yes
Observations	147	147	31	31	31	31
R ²	0.76	0.76	0.67	0.67	0.94	0.96